

PETAK, 29.5.2020. 6.c

Dragi moji,

kraj je tjedna i pravo je vrijeme da se malo zaokruži, završi, stavi točka na „i“,...

Stoga još jednom ukratko – o zagradama i razlomcima u jednadžbama.

Primjer 1: Riješi jednadžbu:

$$-(2x + 8) + 4(-2x + 3) = 1 + (-5x + 3)$$

Najprije se „oslobađamo zagrada“. To radimo na 3 načina:

1. Ako je ispred zgrade samo znak +, prepisujemo članove unutar zgrade sa svojim predznacima, a zgrade obrišemo
2. Ako je ispred zgrade samo znak -, prepisujemo članove unutar zgrade sa suprotnim predznacima, a zgrade obrišemo
3. Ako se zagrada množi s nekim brojem, tada se svaki član u zgradi pomnoži s tim brojem (distributivnost!). $3(2x-5) = 3 \cdot (2x-5)$

Dakle,

$$-(2x + 8) + 4(-2x + 3) = 1 + (-5x + 3)$$

$$-2x - 8 + 4 \cdot (-2x) + 4 \cdot 3 = 1 - 5x + 3 \quad \text{sredimo}$$

$$\underline{-2x - 8} - \underline{8x} + \underline{12} = \underline{1 - 5x} + \underline{3} \quad \text{podvucimo na jedan način poznate članove, a na drugi način nepoznate članove,}$$

razvrstajmo (pazi na promjenu predznaka kada je potrebno)

$$\underline{-2x - 8x} + 5x = \underline{1 + 3 + 8} - 12$$

$$-10x + 5x = 12 - 12$$

$$-5x = 0 / : (-5)$$

$$x = 0$$

Primjer 2 : Riješite jednađbu:

$$\frac{5}{2} - \frac{x}{6} = -\frac{2}{3} \quad / \cdot 6$$

množimo obje strane jednakosti s najmanjim zajedničkim višekratnikom nazivnika $V(2, 6, 3) = 6$

$$\cancel{6}^3 \cdot \frac{5}{\cancel{2}} - \cancel{6}^1 \cdot \frac{x}{\cancel{6}} = \cancel{6}^2 \cdot \left(-\frac{2}{\cancel{3}}\right)$$

svaki član jednađbe množimo sa 6

$$15 - x = -4$$

$$-x = -4 - 15$$

$$-x = -19 \quad / : (-1)$$

$$x = 19$$

Vaše aktivnosti:

1. Dva primjera koja ćete prepisati u bilježnicu:

Primjer 3 : Riješite jednađbu:

$$\frac{x-5}{4} - \frac{2x+2}{8} = 3x \quad / \cdot 8$$

$$V(4, 8) = 8$$

svaki član jednađbe množimo s 8

$$\cancel{8}^2 \cdot \frac{x-5}{\cancel{4}} - \cancel{8}^1 \cdot \frac{2x+2}{\cancel{8}} = 8 \cdot 3x$$

$$2(x-5) - 1(2x+2) = 24x$$

$$2x - 10 - 2x - 2 = 24x$$

$$2x - 2x - 24x = 2 + 10$$

$$-24x = 12 \quad / : (-24)$$

$$x = -\frac{\cancel{12}^1}{\cancel{24}_2} = -\frac{1}{2}$$

Primjer 4: Riješite jednađbu:

$$\frac{2x+3}{3} - 3 = \frac{3x-3}{5} - \frac{x-6}{2} + \frac{2x-12}{5} \quad / \quad 30$$

$30 : 3 = 10$ $30 : 5 = 6$ $30 : 2 = 15$ $30 : 5 = 6$

$$10(2x+3) - 90 = 6(3x-3) - 15(x-6) + 6(2x-12)$$
$$20x + 30 - 90 = 18x - 18 - 15x + 90 + 12x - 72$$
$$20x - 18x + 15x - 12x = -72 + 90 - 18 + 90 - 30$$
$$5x = 60$$
$$x = 12$$

2. Riješite kviz.

Kviz je obavezna vježba, može se riješiti 29.5.2020. od 8 do 23:59.

<https://forms.office.com/Pages/ResponsePage.aspx?id=FvJamzTGgEurAgyaPQKQka9gUnItaLdLqbvUmbRz--xUQIVOU1NNOEJHTjc0MIBNUIRZVDJHOVZZRS4u>

3. Zadatak: Samostalno riješite jednađbe:

a) $-\frac{1}{5}x - 2 = 3x - \frac{2}{5}$

b) $\frac{3x-5}{2} = \frac{2}{3} + x$

c) $\frac{x+5}{2} - \frac{1-x}{4} = \frac{9+2x}{3} - 1$

$$d) \frac{x+1}{3} - \frac{x}{4} = \frac{1}{2}$$

$$e) 7(2x - 1) - (5x - 4) + (9 - 7x) = 0$$

Poslikajte bilježnicu te mi rješenja ovih 5 zadataka (a,b,c,d,e) pošaljite do nedjelje navečer na mail matematikasever@gmail.com

IND: isto

Po potrebi si pogledajte video lekciju Tonija Miluna <https://www.youtube.com/watch?v=rHQbw3CccJQ> ali ne sve, nego od 21:40 – 48:09 (samo taj dio videa, dakle otprilike od 21. do 48. minute videa).

Rješenja prethodne domaće zadaće - ispod

Zadatok 1.

$$\begin{aligned} \text{a)} \quad & 3 - (5 - x) = 14 \\ & 3 - 5 + x = 14 \\ & x = 14 - 3 + 5 \\ & x = 19 - 3 \\ & \boxed{x = 16} \end{aligned}$$

$$\begin{aligned} \text{b)} \quad & 2x + (3 - 4x) = 5x - 11 \\ & \underline{2x} + 3 - \underline{4x} = \underline{5x} - 11 \\ & 2x - 4x - 5x = -11 + 3 \\ & 2x - 9x = -14 \\ & -7x = -14 \quad /: (-7) \\ & \boxed{x = \frac{-14}{-7} = 2} \end{aligned}$$

$$\begin{aligned} \text{c)} \quad & 5 \cdot (2x - 11) - 6 = 39 \\ & \underline{5 \cdot 2x} - \underline{5 \cdot 11} - 6 = 39 \\ & 10x - 55 - 6 = 39 \\ & 10x = 39 + 55 + 6 \\ & 10x = 100 \quad /: 10 \\ & \boxed{x = \frac{100}{10} = 10} \end{aligned}$$

$$\begin{aligned} \text{d)} \quad & 2 \cdot (x + 5) = 8 \cdot (x + 2) \\ & \underline{2 \cdot x} + \underline{2 \cdot 5} = \underline{8 \cdot x} + \underline{8 \cdot 2} \\ & 2x + 10 = 8x + 16 \\ & 2x - 8x = 16 - 10 \\ & -6x = 6 \quad /: (-6) \\ & x = \frac{6}{-6} \\ & \boxed{x = -1} \end{aligned}$$

PROVJERA

$$\begin{aligned} & 3 - (5 - 16) = 14 \\ & 3 - 5 + 16 = 14 \\ & 19 - 5 = 14 \\ & 14 = 14 \quad \checkmark \end{aligned}$$

PROVJERA

$$\begin{aligned} & 2 \cdot 2 + (3 - 4 \cdot 2) = 5 \cdot 2 - 11 \\ & 4 + (3 - 8) = 10 - 11 \\ & 4 + (-5) = -1 \\ & -1 = -1 \quad \checkmark \end{aligned}$$

PROVJERA

$$\begin{aligned} & 5 \cdot (2 \cdot 10 - 11) - 6 = 39 \\ & 5 \cdot (20 - 11) - 6 = 39 \\ & 5 \cdot 9 - 6 = 39 \\ & 45 - 6 = 39 \\ & 39 = 39 \quad \checkmark \end{aligned}$$

PROVJERA

$$\begin{aligned} & 2 \cdot (-1 + 5) = 8 \cdot (-1 + 2) \\ & 2 \cdot 4 = 8 \cdot 1 \\ & 8 = 8 \quad \checkmark \end{aligned}$$

$$e) \quad 3(-5x+15)+45 = -8(5x-15) \rightarrow 3 \cdot (-5x) + 3 \cdot 15 + 45 = -8 \cdot 5x - 8 \cdot (-15)$$

$$-15x + 45 + 45 = -40x + 120 \quad \leftarrow 3 \cdot (-5) \cdot x = -15x$$

$$-15x + 40x = 120 - 45 - 45$$

$$25x = 30 \quad | : 25$$

$$x = \frac{30}{25} = \frac{6}{5} = 1\frac{1}{5}$$

PROVJERA

$$3 \cdot \left(-5 \cdot \frac{6}{5} + 15\right) + 45 = -8 \cdot \left(5 \cdot \frac{6}{5} - 15\right)$$

$$3 \cdot (-6 + 15) + 45 = -8(6 - 15)$$

$$3 \cdot 9 + 45 = -8 \cdot (-9)$$

$$27 + 45 = 72$$

$$72 = 72 \quad \checkmark$$

$$f) \quad 2(2x-3)-1 = -9-3(-x+4)+10$$

$$4x - 6 - 1 = -9 + 3x - 12 + 10$$

$$4x - 3x = -9 - 12 + 10 + 6 + 1$$

$$x = -21 + 17$$

$$\boxed{x = -4}$$

$$g) \quad 8 - (-2x+4) = -2(3x-2) + (-x-1)$$

$$8 + 2x - 4 = -6x + 4 - x - 1$$

$$2x + 6x + x = 4 - 1 - 8 + 4$$

$$9x = 8 - 9$$

$$9x = -1 \quad | : 9$$

$$\boxed{x = \frac{-1}{9}}$$

$$h) \quad 2(y+7) = -5(1-y) + 19$$

$$2y + 14 = -5 + 5y + 19$$

$$2y - 5y = -5 + 19 - 14$$

$$-3y = 19 - 19$$

$$-3y = 0 \quad | : (-3)$$

$$y = \frac{0}{-3}$$

$$\boxed{y = 0}$$

DOMAĆA ZADAĆA, zad. 16. str. 134

$$\frac{3x}{5} = \frac{3}{5}x$$

16.) Riješi jednačinu

a) $\frac{3}{4}x - \frac{3}{2} = \frac{3}{8} \quad | \cdot 8 \quad v(4,2,8)=8$

$$\overset{2}{\cancel{8}} \cdot \frac{3}{\underset{1}{4}}x - \overset{4}{\cancel{8}} \cdot \frac{3}{\underset{1}{2}} = \overset{1}{\cancel{8}} \cdot \frac{3}{\underset{1}{8}}$$

$$2 \cdot 3x - 4 \cdot 3 = 1 \cdot 3$$

$$6x - 12 = 3$$

$$6x = 3 + 12$$

$$6x = 15 \quad | : 6$$

$$x = \frac{15}{6} = \frac{5}{2} = 2\frac{1}{2}$$

b) $\frac{2}{9} + \frac{5}{6}x - \frac{3}{2} = \frac{1}{3} \quad | \cdot 18 \quad v(9,6,2,3)=18$

$$\overset{2}{\cancel{18}} \cdot \frac{2}{\underset{1}{9}} + \overset{3}{\cancel{18}} \cdot \frac{5}{\underset{1}{6}}x - \overset{9}{\cancel{18}} \cdot \frac{3}{\underset{1}{2}} = \overset{6}{\cancel{18}} \cdot \frac{1}{\underset{1}{3}}$$

$$4 + 15x - 27 = 6$$

$$15x = 6 - 4 + 27$$

$$15x = 33 - 4$$

$$15x = 29 \quad | : 15$$

$$x = \frac{29}{15} = 1\frac{14}{15}$$

c) $\frac{5}{6} - 2x + \frac{3}{2} = \frac{3}{4} - \frac{x}{3} \quad | \cdot 12 \quad \frac{x}{3} = \frac{1}{3}x \quad !!!$

$$\overset{2}{\cancel{12}} \cdot \frac{5}{\underset{1}{6}} - \overset{12}{\cancel{12}} \cdot 2x + \overset{6}{\cancel{12}} \cdot \frac{3}{\underset{1}{2}} = \overset{3}{\cancel{12}} \cdot \frac{3}{\underset{1}{4}} - \overset{4}{\cancel{12}} \cdot \frac{x}{\underset{1}{3}}$$

$$10 - 24x + 18 = 9 - 4x$$

$$-24x + 4x = 9 - 10 - 18$$

$$-20x = 9 - 28$$

$$-20x = -19 \quad | : (-20)$$

$$x = \frac{-19}{-20} = \frac{19}{20}$$

d) $\frac{5}{3}x - \frac{1}{6} + x = \frac{4}{5}x - \frac{3}{2} \quad | \cdot 30 \quad v(3,6,5,2)=30$

$$\overset{10}{\cancel{30}} \cdot \frac{5}{\underset{1}{3}}x - \overset{5}{\cancel{30}} \cdot \frac{1}{\underset{1}{6}} + \overset{30}{\cancel{30}} \cdot x = \overset{6}{\cancel{30}} \cdot \frac{4}{\underset{1}{5}}x - \overset{15}{\cancel{30}} \cdot \frac{3}{\underset{1}{2}}$$

$$50x - 5 + 30x = 24x - 45$$

$$50x + 30x - 24x = -45 + 5$$

$$80x - 24x = -40$$

$$56x = -40 \quad | : 56$$

$$x = \frac{-40}{56} = \frac{-5}{7}$$

$$e) 2\frac{1}{4} + 2x - \frac{7}{9} - \frac{1}{6}x = \frac{2x}{3} \quad \boxed{\frac{2x}{3} = \frac{2}{3}x}$$

$$\frac{9}{4} + 2x - \frac{7}{9} - \frac{7}{6}x = \frac{2x}{3} \quad / \cdot 36$$

$$\overset{9}{36} \cdot \frac{9}{4} + 36 \cdot 2x - \overset{4}{36} \cdot \frac{7}{9} - \overset{6}{36} \cdot \frac{7}{6}x = \overset{12}{36} \cdot \frac{2x}{3}$$

$$81 + 72x - 28 - 42x = 24x$$

$$72x - 42x - 24x = -81 + 28$$

$$72x - 66x = -53$$

$$6x = -53 \quad / : 6$$

$$\boxed{x = \frac{-53}{6} = -8\frac{5}{6}}$$

$$f) \frac{3}{5}x + 1\frac{5}{6} - \frac{2}{15} = x + 1\frac{3}{4} \quad \begin{array}{l|l} 5, 6, 15, 4 & 2 \\ 5, 3, 15, 2 & 2 \\ 5, 3, 15, 1 & 5 \\ 1, 3, 3, 1 & 3 \\ 1, 1, 1, 1 & 2 \cdot 2 \cdot 5 \cdot 3 = 60 \end{array}$$

$$\frac{3}{5}x + \frac{11}{6} - \frac{2}{15} = x + \frac{7}{4} \quad / \cdot 60$$

$$\overset{12}{60} \cdot \frac{3}{5}x + \overset{10}{60} \cdot \frac{11}{6} - \overset{4}{60} \cdot \frac{2}{15} = 60 \cdot x + \overset{15}{60} \cdot \frac{7}{4}$$

$$36x + 110 - 8 = 60x + 105$$

$$36x - 60x = 105 - 110 + 8$$

$$-24x = 113 - 110$$

$$-24x = 3 \quad / : (-24)$$

$$\boxed{x = \frac{3}{-24} = -\frac{1}{8}}$$

$$g) \frac{5}{12}x - \frac{x}{8} + 1\frac{2}{3} = 2\frac{1}{2} + \frac{3x}{4} - \frac{7}{6}$$

$$\frac{5}{12}x - \frac{x}{8} + \frac{5}{3} = \frac{5}{2} + \frac{3x}{4} - \frac{7}{6} \quad / \cdot 24$$

$$\overset{2}{24} \cdot \frac{5}{12}x - \overset{3}{24} \cdot \frac{x}{8} + \overset{8}{24} \cdot \frac{5}{3} = \overset{12}{24} \cdot \frac{5}{2} + \overset{6}{24} \cdot \frac{3x}{4} - \overset{4}{24} \cdot \frac{7}{6}$$

$$10x - 3x + 40 = 60 + 18x - 28$$

$$10x - 3x - 18x = 60 - 28 - 40$$

$$10x - 21x = 60 - 68$$

$$-11x = -8 \quad / : (-11)$$

$$\boxed{x = \frac{-8}{-11} = \frac{8}{11}}$$

$$h) \frac{3x}{2} - \frac{1}{6} - \frac{1}{4}x + \frac{1}{3} - 2x = \frac{4}{5} - x - \frac{3}{10}$$

$$\frac{3x}{2} - \frac{1}{6} - \frac{5}{4}x + \frac{4}{3} - 2x = \frac{4}{5} - x - \frac{3}{10} \quad / \cdot 60$$

$$90x - 10 - 75x + 80 - 120x = 48 - 60x - 18$$

$$90x - 75x - 120x + 60x = 48 - 18 + 10 - 80$$

$$150x - 195x = 58 - 98$$

$$-45x = -40 \quad / : (-45)$$

$$x = \frac{-40}{-45}$$

$$\boxed{x = \frac{8}{9}}$$

$$\boxed{\frac{x}{8} = \frac{1}{8}x}$$

$$\boxed{\frac{-x}{5} = -\frac{1}{5}x}$$

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